

2025Q4

MASS & ENERGY BALANCES WITH FLOW RATES

LEVEL 1 QUESTION (GRADES 5 – 8)

Solution: Mass Flow Rate

The problem states that a fan moves a mass of air (40 kg) over a period of 8 seconds.

Step 1: Use the Mass Flow Rate Equation

$$\dot{m} = \frac{\text{Mass (kg)}}{\text{Time (s)}}$$

$$\dot{m} = \frac{40 \text{ kg}}{8 \text{ s}}$$

$$\dot{m} = \frac{5 \text{ kg}}{1 \text{ s}}$$

$$\dot{m} = 5 \text{ kg/s}$$

This means that the fan moves 5 kg of air per second.

Step 2: Unit Conversion to the Required Units (lb/s)

The question requires the answer in pounds per second, instead of kilogram per second. Thus, a unit conversion is necessary. The hint states that 1kg = 2.2 lbs.

$$\dot{m} = \frac{5 \cancel{\text{kg}}}{\text{s}} \times \frac{2.2 \text{ lb}}{1 \cancel{\text{kg}}}$$

The kg units in the numerator and denominator will cancel out.

$$\dot{m} = \frac{11 \text{ lb}}{1 \text{ s}}$$

$$\dot{m} = 11 \text{ lb/s}$$

Final Answer: 11 pounds per second (11 lb/s)

LEVEL 2 QUESTION (GRADES 8 –11)

Solution: Volumetric Flow Rate -> Mass Flow rate

The problem requires calculating the volumetric flow rate, converting the volumetric flow rate to the mass flow rate using air density, followed by a unit conversion.

Step 1: Calculating Volumetric Flow Rate

Remember to convert minutes to seconds.

$$Q = \frac{24m^3}{2 \cancel{min}} \times \frac{1 \cancel{min}}{60 s}$$

$$Q = \frac{24 m^3}{120 s}$$

$$Q = \frac{1 m^3}{5 s}$$

$$Q = 0.2 m^3/s$$

Step 2: Calculating Mass Flow Rate using Q and ρ

$$\dot{m} = \rho \times Q$$

$$\dot{m} = \frac{1.225 kg}{\cancel{m^3}} \times 0.2 \frac{\cancel{m^3}}{s}$$

$$\dot{m} = 0.245 kg/s$$

Step 3: Unit Conversion to the Required Units (lb/s)

$$\dot{m} = \frac{0.245 \cancel{kg}}{s} \times \frac{2.2 lb}{1 \cancel{kg}}$$

$$\dot{m} = 0.539 lb/s$$

Final Answer: 0.539 pounds per second (0.539 lb/s)